

A circle is the set of all points  $(x, y)$  in a plane equidistant from a fixed point  $(h, k)$  called the **center** of the circle. The distance,  $r$ , between the center and any point  $(x, y)$  on the circle is the **radius**.

Standard Form Equation for a circle with center  $(h, k)$  and radius  $r$  is:  $(x - h)^2 + (y - k)^2 = r^2$

Find the equation of the circle containing point  $(1, 4)$  with a center at  $(-2, -3)$ .

Using the distance formula:  $r = \sqrt{(1 + 2)^2 + (4 + 3)^2} = \sqrt{9 + 49} = \sqrt{58} \rightarrow \boxed{(x + 2)^2 + (y + 3)^2 = 58}$

A parabola is the set of points  $(x, y)$  in a plane that are equidistant from a fixed line, the **directrix**, and a fixed point, the **focus**, not on the directrix. The midpoint between the focus and the directrix is the **vertex**, and the line passing through the focus and the vertex is the **axis of symmetry**.

Standard Form Equation of a parabola with horizontal directrix  $y = k - p$  is:  $(x - h)^2 = 4p(y - k)$ ,  $p \neq 0$

Standard Form Equation of a parabola with vertical directrix  $x = h - p$  is:  $(y - k)^2 = 4p(x - h)$ ,  $p \neq 0$

In each case,  $p$  is the directed distance from the vertex to the focus.

Find the standard equation of the parabola with vertex at  $(0, 0)$  and focus at  $(0, 4)$ .

The axis of symmetry is vertical and the directrix is horizontal, so we get:  $x^2 = 4py$  but the directed distance from the vertex to the focus is  $+4$ ,  $p = 4$  so we get:  $\boxed{x^2 = 16y}$

Another form if we want  $y$  as a function of  $x$ , would be  $\boxed{y = \frac{1}{16}x^2}$

1. Find the equation of the circle with center  $(0, 0)$  and radius  $4\sqrt{2}$ .

2. Find the equation of the circle with center  $(5, -6)$  and diameter  $4\sqrt{3}$ .

3. Find the center and radius of the circle:  $(x + 9)^2 + (y + 1)^2 = 36$

4. Find the center and radius of the circle:  $x^2 + (y + 12)^2 = 24$

5. Write the equation of the circle in standard form:  $\frac{1}{9}x^2 + \frac{1}{9}y^2 = 1$

6. Write the equation of the circle in standard form:  $\frac{1}{9}x^2 + \frac{1}{9}y^2 = 1$

7. Find the Vertex, Focus, and Directrix of the parabola:  $y = -4x^2$

8. Find the Vertex, Focus, and Directrix of the parabola:  $(x - 5) + (y + 4)^2 = 0$

9. Find the Vertex, Focus, and Directrix of the parabola:  $(x - 5) + (y + 4)^2 = 0$

10. Find the Vertex, Focus, and Directrix of the parabola:  $y^2 - 4y - 4x = 0$

11. Find the standard equation for the parabola with vertex  $(3, -3)$  and focus  $(3, -9/4)$

12. Find the standard equation for the parabola with vertex  $(2, 2)$  and directrix  $x = -2$ .