

1. Write an infinite repeating decimal using Sigma, then Find the Exact value.as a convergent infinite series.

Solution:

$$5.2323232323\dots = 5. + 0.23 + 0.0023 + 0.000023 + 0.00000023 + \dots$$

After the 5, the rest is a geometric series where $a_1 = 0.23$ and $r = 0.01$

So we can get:
$$5 + \sum_{n=1}^{\infty} 2.3(0.01)^{n-1} = 5 + \frac{0.23}{1-0.01} = 5 + \frac{0.23}{0.99} = 5 + \frac{23}{99} = \boxed{\frac{518}{99}}$$

2. Arithmetic Means

Find the 2 arithmetic means between 5 and 10.

This means we have an arithmetic sequence: 5, a_2 , a_3 , 10, where we must find a_2 and a_3 .

$$a_n = a_1 + (n - 1)d \rightarrow a_4 = 5 + (3)d = 10 \rightarrow 3d = 5 \rightarrow d = \frac{5}{3}$$

$$a_2 = 5 + \frac{5}{3} = \frac{20}{3} \quad \text{and} \quad a_3 = \frac{20}{3} + \frac{5}{3} = \frac{25}{3}$$

3. To find geometric means, follow the same procedure, except use the general term for a geometric term.
4. At this point you should be able to do the following:
- Find Arithmetic Means
 - Find Geometric Means
 - Find The Exact Value of an Infinite Repeating Decimal
 - Given 2 values of a sequence, find a random 3rd term
 - Find the number of terms in a sequence, given a particular term, r or d , and the sum
 - Express a sum of terms in summation notation form

Calculators may be used.

$$1. \sum_{n=1}^{20} 2n + 1 =$$

$$2. \sum_{n=1}^{100} \frac{n+1}{2} =$$

3. In an arithmetic sequence, $a_4 = 7$ and $a_9 = 20$. Find a_{101} .

$$4. \sum_{n=1}^8 3(2)^n =$$

$$5. \sum_{n=0}^{30} 3\left(\frac{3}{2}\right)^n =$$

$$6. \sum_{n=0}^{\infty} 6\left(\frac{2}{3}\right)^n =$$

$$7. \sum_{n=0}^{\infty} 10\left(\frac{4}{5}\right)^n =$$

$$8. \sum_{n=1}^{\infty} 8\left(\frac{5}{3}\right)^{n-1} =$$

$$9. 9 + 6 + 4 + \frac{8}{3} + \dots =$$

$$10. -6 + 5 - \frac{25}{6} + \frac{125}{36} - \dots =$$