

Operation Identity:

$$3 \cdot 1 = 3$$

$$4 + 0 = 4$$

$$x \cdot 1 = x$$

$$w + 0 = w$$

1 is the multiplicative identity for real numbers

0 is the additive identity for real numbers

Find  $w$ ,  $x$ ,  $y$ , and  $z$ :

$$\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix} * \begin{bmatrix} w & x \\ y & z \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$

$$\begin{bmatrix} (2w + y) & (2x + z) \\ (4w + 3y) & (4x + 3z) \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$

$$\begin{cases} 2w + y = 2 \\ 4w + 3y = 4 \end{cases} \quad \text{and} \quad \begin{cases} 2x + z = 1 \\ 4x + 3z = 3 \end{cases}$$

$$w = 1$$

$$x = 0$$

$$y = 0$$

$$z = 1$$

$$\begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix} * \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$

$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  is the **Multiplicative Identity** for any **2 by 2 matrix**.

What would be the Multiplicative Identity for any 3 by 3 matrix?

Demonstrate your conclusion by multiplying it by  $\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$ .

## Inverses

$$2 * \frac{1}{2} = 1$$

Since the multiplication results in the Multiplicative Identity,

2 and  $\frac{1}{2}$  are **Multiplicative Inverses** of each other.

$$4 + (-4) = 0$$

Since the Addition results in the Additive Identity,

4 and -4 are **Additive Inverses** of each other.

Find the Multiplicative Inverse of  $\begin{bmatrix} 4 & 1 \\ 2 & 3 \end{bmatrix}$  Use Decimals

$$\begin{bmatrix} 4 & 1 \\ 2 & 3 \end{bmatrix} * \begin{bmatrix} w & x \\ y & z \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$\begin{bmatrix} 0.3 & -0.1 \\ -0.2 & 0.4 \end{bmatrix}$  is the Multiplicative Inverse, because

$$\begin{bmatrix} 4 & 1 \\ 2 & 3 \end{bmatrix} * \begin{bmatrix} 0.3 & -0.1 \\ -0.2 & 0.4 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

Find the Multiplicative Inverse of  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$  Call it  $\begin{bmatrix} w & x \\ y & z \end{bmatrix}$

Answer:

$$\begin{bmatrix} \frac{d}{ad - bc} & \frac{-b}{ad - bc} \\ \frac{-c}{ad - bc} & \frac{a}{ad - bc} \end{bmatrix}$$

Note the Pattern:

Switch elements on the Primary Diagonal.

Switch signs on the Secondary Diagonal.

Divide Each by the Determinant of the Original Matrix.

Find the Multiplicative Inverse of  $\begin{bmatrix} 8 & 4 \\ 4 & 2 \end{bmatrix}$

This Matrix is Not Invertible = No Inverse Exists

Multiplicative Identities:

2 x 2

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

3 x 3

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

4 x 4

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

5 x 5

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Find the Multiplicative Inverse of each 2 x 2 Matrix.

1.  $\begin{bmatrix} 2 & 0 \\ 0 & 3 \end{bmatrix}$

2.  $\begin{bmatrix} 1 & -2 \\ 2 & -3 \end{bmatrix}$

3.  $\begin{bmatrix} 1 & 2 \\ 3 & 7 \end{bmatrix}$

4.  $\begin{bmatrix} -7 & 33 \\ 4 & -19 \end{bmatrix}$

5.  $\begin{bmatrix} 5 & 1 \\ -2 & -2 \end{bmatrix}$

6. 
$$\begin{bmatrix} \frac{1}{4} & \frac{2}{3} \\ \frac{1}{3} & \frac{8}{9} \end{bmatrix}$$

7. 
$$\begin{bmatrix} 2 & 3 \\ -1 & 5 \end{bmatrix}$$

8. 
$$\begin{bmatrix} 1 & -2 \\ -3 & 2 \end{bmatrix}$$

9. 
$$\begin{bmatrix} -1 & 0 \\ 3 & -2 \end{bmatrix}$$

10. 
$$\begin{bmatrix} 2 & -5 \\ 3 & 1 \end{bmatrix}$$