

To Add 2 Matrices, they must be exactly of the same dimension: equal number of rows and equal number of columns.

$$\begin{bmatrix} 2 & -1 & 3 \\ 8 & -6 & 4 \\ 0 & 1 & 5 \\ 7 & -7 & 9 \end{bmatrix} + \begin{bmatrix} 3 & -5 & 4 \\ 1 & 0 & 3 \\ -3 & -5 & -3 \\ -7 & 9 & -4 \end{bmatrix} = \begin{bmatrix} 5 & -6 & 7 \\ 9 & -6 & 7 \\ -3 & -4 & 2 \\ 0 & 2 & 5 \end{bmatrix}$$

To Multiply 2 Matrices, the number of columns of the 1st must equal the number of rows of the 2nd and the result has the number of rows of the 1st and the numbers of columns of the 2nd.

$$\begin{bmatrix} 1 & 0 & 3 \\ 2 & -1 & -2 \end{bmatrix} * \begin{bmatrix} -2 & 4 & 2 \\ 1 & 0 & 0 \\ -1 & 1 & -1 \end{bmatrix} = \begin{bmatrix} -5 & 7 & -1 \\ -3 & 6 & 6 \end{bmatrix}$$

Only Square Matrices have Determinants. If A is a Square Matrix, the **Minor** M_{ij} of the entry a_{ij} is the determinant of the matrix obtained by deleting the i^{th} row and the j^{th} column of A.

The **Cofactor** C_{ij} of the entry a_{ij} is given by $C_{ij} = (-1)^{i+j}M_{ij}$

$$A = \begin{bmatrix} 0 & 2 & 1 \\ 3 & -1 & 2 \\ 4 & 0 & 1 \end{bmatrix} \text{ The Minor of } -1 \text{ is } \begin{vmatrix} 0 & 1 \\ 4 & 1 \end{vmatrix} = 0 - 4 = -3$$

To find the Determinant of a square matrix, pick a row or a column and multiply each element by its Cofactor and add the results.

$$\begin{aligned} \text{The determinant of } \begin{bmatrix} 0 & 2 & 1 \\ 3 & -1 & 2 \\ 4 & 0 & 1 \end{bmatrix} &= \begin{vmatrix} 0 & 2 & 1 \\ 3 & -1 & 2 \\ 4 & 0 & 1 \end{vmatrix} = -3 \begin{vmatrix} 2 & 1 \\ 0 & 1 \end{vmatrix} - \begin{vmatrix} 0 & 1 \\ 4 & 1 \end{vmatrix} - 2 \begin{vmatrix} 0 & 2 \\ 4 & 0 \end{vmatrix} \\ &= -3(2) - (-4) - 2(-8) = -6 + 4 + 16 = 14 \end{aligned}$$

1. Find the Determinant of $\begin{bmatrix} 1 & 2 & 1 \\ 2 & -1 & 0 \\ 3 & 0 & 2 \end{bmatrix}$

2. Multiply: $\begin{bmatrix} 2 & 3 & -1 \\ 1 & 3 & 2 \end{bmatrix} * \begin{bmatrix} 3 & 4 \\ -2 & 2 \\ 1 & -1 \end{bmatrix} =$

3. $\begin{bmatrix} 3 & -5 \\ 4 & 1 \end{bmatrix} - \begin{bmatrix} 4 & 3 \\ 5 & -2 \end{bmatrix} =$

4. $\begin{bmatrix} 2 & 8 \\ 3 & 7 \end{bmatrix} * 2 \begin{bmatrix} 4 \\ 1 \end{bmatrix} =$