

1. DeMoivre's Theorem:  $(r \operatorname{cis} \theta)^n = r^n \operatorname{cis} n\theta$  (Take  $r$  to the  $n^{\text{th}}$  power, then  $n$  times  $\theta$ )

2. DeMoivre's Theorem can be used to easily find higher powers of complex numbers.

$(3 + 3\sqrt{3}i)^5$  would take a lot of steps if we multiplied the binomial a number of times.

Switch to Trigonometric Form:  $r = \sqrt{9+27} = 6$   $\theta = \arctan \frac{3\sqrt{3}}{3} = \arctan \sqrt{3} = \frac{\pi}{3} = 60^\circ$

Using DeMoivre's Theorem, we get  $r = 6^5 = 7776$   $5\theta = \frac{5\pi}{3} = 300^\circ \rightarrow 7776 \operatorname{cis} \frac{5\pi}{3} = 7776 \operatorname{cis} 300^\circ$ .

Convert back to Standard Form:  $7776 \cos \frac{5\pi}{3} + 7776 \sin \frac{5\pi}{3} i = (7776) \frac{1}{2} - (7776) \frac{\sqrt{3}}{2} i = \boxed{3888 - 3888\sqrt{3}i}$

Use DeMoivre's Theorem to find the indicated power of the complex number. Write the result in standard form.

1.  $(1 + i)^3$

2.  $(2 + 2i)^6$

3.  $(-1 + i)^{10}$

4.  $(1 - i)^8$

5.  $2(\sqrt{3} + i)^5$

6.  $4(1 - \sqrt{3}i)^3$

7.  $(5 \operatorname{cis} 20^\circ)^3$

8.  $(3 \operatorname{cis} 150^\circ)^4$

9.  $\left(2 \operatorname{cis} \frac{\pi}{2}\right)^{12}$

10.  $(2 \operatorname{cis} \pi)^8$

11.  $(\operatorname{cis} 0)^{20}$

12.  $(4 \operatorname{cis} 10^\circ)^6$

13.  $(3 \operatorname{cis} 15^\circ)^4$

14.  $\left(3 \operatorname{cis} \frac{\pi}{8}\right)^2$

15.  $\left[2\left(\cos \frac{\pi}{10} + i \sin \frac{\pi}{10}\right)\right]^5$