

1. Polar Form of a vector gives its magnitude and direction. For the magnitude we will typically use the variable r . For the direction we will typically use the variable θ .

2. Polar Form will be $\langle r, \theta \rangle$ and Rectangular Form will be $\langle x, y \rangle$

3. The equations needed for conversion between the 2 forms are:

$$x = r \cos \theta, \quad y = r \sin \theta, \quad r = \sqrt{x^2 + y^2}, \quad \theta = \arctan \frac{y}{x}$$

4. Convert the Polar Form $\langle 27, 49^\circ \rangle$ to Rectangular form:

$$x = r \cos \theta \quad \text{and} \quad y = r \sin \theta. \quad \text{Therefore we compute } \langle 27 \cos 49^\circ, 27 \sin 49^\circ \rangle = \boxed{\langle 17.714, 20.377 \rangle}$$

5. Convert Rectangular Form $\langle 57, -129 \rangle$ to Polar Form:

$$r = \sqrt{x^2 + y^2} \quad \text{and} \quad \theta = \arctan \frac{y}{x}. \quad \text{Therefore we compute } \langle \sqrt{57^2 + 129^2}, \arctan \frac{-129}{57} \rangle \\ = \boxed{\langle 141.032, 293.839^\circ \rangle}$$

6. A 7000 pound vehicle is on a 25° incline.

Find the component vector acting on a perpendicular to the incline in Rectangular form.

Find the component vector acting on a perpendicular to the incline in Polar Form.

The force due to gravity is $\mathbf{f} = \langle 0, -7000 \rangle$

Two unit vectors along the incline are $\vec{U} = \langle \cos 10^\circ, \sin 10^\circ \rangle$ and $\vec{D} = \langle \cos 190^\circ, \sin 190^\circ \rangle$.

The downward unit vector perpendicular to the incline is $\mathbf{p} = \langle \cos 280^\circ, \sin 280^\circ \rangle$.

$$\text{Calculate: } \text{proj}_{\mathbf{p}} \mathbf{f} = \frac{\mathbf{p} \cdot \mathbf{f}}{\|\mathbf{p}\|^2} \mathbf{p} = \frac{\langle \cos 280^\circ, \sin 280^\circ \rangle \bullet \langle 0, -7000 \rangle}{1} \langle \cos 280^\circ, \sin 280^\circ \rangle.$$

$$= -7000 \sin 280^\circ \langle \cos 280^\circ, \sin 280^\circ \rangle = \boxed{\langle 1197.071, -6788.924 \rangle} \quad \text{Rectangular Form}$$

$$r = \sqrt{1197.071^2 + 6788.924^2} = 6893.654 \quad \text{and} \quad \theta = 280^\circ \quad \boxed{\langle 6893.654, 280^\circ \rangle} \quad \text{Polar Form}$$

1. Find the angle between $\vec{u} = \langle 2, -3 \rangle$ and $\vec{v} = \langle 1, -2 \rangle$.

2. How much force is necessary to prevent a 5000-pound vehicle from rolling down a 10° incline.

3. An 850-pound motorcycle is parked on a 5° incline. Find the force component perpendicular to the incline.

4. Force $\vec{F} = \langle 29, 51 \rangle$ moves an object from $(3, 9)$ to $(7, 41)$. Find the work done.

5. Find the Projection of $\vec{u} = \langle 6, -2 \rangle$ onto $\vec{v} = \langle 22, -7 \rangle$.

6. Given in Polar Form, $\vec{v} = \langle 41, 22^\circ \rangle$. Convert to Rectangular Form.

7. Given in Rectangular Form, $\vec{v} = \langle 71, 22 \rangle$. Convert to Polar Form.

8. Given $\vec{u} = \langle 29, 40^\circ \rangle$ and $\vec{v} = \langle 99, 91^\circ \rangle$. Find the dot product $\vec{u} \cdot \vec{v}$.

9. Find the work done by Force \vec{F} with magnitude 55 and direction 18° , acting on an object with displacement from $(14, 22)$ to $(20, 30)$.

10. In Polar Form, $\vec{u} = \langle 14, 60^\circ \rangle$ and $\vec{v} = \langle 23, 17^\circ \rangle$. Find $\vec{u} + \vec{v}$ in Polar Form.