


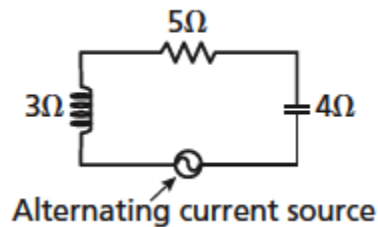


Electrical circuit components, such as resistors, inductors, and capacitors, all oppose the flow of current. This opposition is called *resistance* for resistors and *reactance* for inductors and capacitors. Each of these quantities is measured in ohms. The symbol used for ohms is  $\Omega$ , the uppercase Greek letter omega.

Component and symbol	Resistor 	Inductor 	Capacitor 
Resistance or reactance (in ohms)	$R$	$L$	$C$
Impedance (in ohms)	$R$	$Li$	$-Ci$



The table shows the relationship between a component's resistance or reactance and its contribution to impedance. A series circuit is also shown with the resistance or reactance of each component labeled. The impedance for a series circuit is the sum of the impedances for the individual components. Find the impedance of the circuit.

*Solution:*

The resistor has a resistance of 5 ohms, so its impedance is 5 ohms. The inductor has a reactance of 3 ohms, so its impedance is  $3i$  ohms. The capacitor has a reactance of 4 ohms, so its impedance is  $-4i$  ohms. Impedance of circuit =  $5 + 3i + (-4i) = 5 - i$

The impedance of the circuit is  $(5 - i)$  ohms.

Multiplication of Complex Numbers:

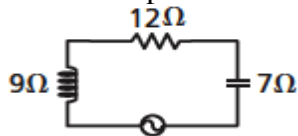
$$\begin{aligned} &4i(-6 + i) \\ &= -24i + 4i^2 \\ &= -24i - 4 \\ &= \boxed{-4 - 24i} \end{aligned}$$

$$\begin{aligned} &(9 - 2i)(-4 + 7i) \\ &= -36 + 63i + 8i - 14i^2 \\ &= -36 + 71i + 14 \\ &= \boxed{22 + 71i} \end{aligned}$$

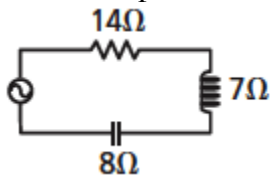
$$\begin{aligned} \text{Solve: } &2x^2 - 11 = -47 \\ &2x^2 = -36 \\ &x^2 = -18 \\ &x = \pm\sqrt{-18} = \pm i\sqrt{18} \\ &\boxed{x = \pm 3i\sqrt{2}} \end{aligned}$$

1.  $(6 - i) + (7 + 3i)$
2.  $(9 + 5i) + (11 + 2i)$
3.  $(12 + 4i) - (3 - 7i)$
4.  $(2 - 15i) - (4 + 5i)$
5.  $(12 - 3i) + (7 + 3i)$
6.  $(16 - 9i) - (2 - 9i)$
7.  $7 - (3 + 4i) + 6i$
8.  $16 - (2 - 3i) - i$
9.  $-10 + (6 - 5i) - 9i$
10.  $-3 + (8 + 2i) + 7i$

11. Find the impedance of the series circuit.



12. Find the impedance of the series circuit.



13.  $3i(-5 + i)$
14.  $2i(7 - i)$
15.  $(7 + 5i)(8 - 6i)$
16.  $(8 + 3i)^2$