

Logarithmic Functions

For $x > 0$, $a > 0$, and $a \neq 1$:

$$y = \log_a x \text{ iff } x = a^y$$

$f(x) = \log_a x$ is called a logarithmic function.

$$\log_2 32 = 5$$

$$\log_3 1 = 0$$

$$\log_4 2 = \frac{1}{2}$$

$$\log_{10} \left(\frac{1}{100} \right) = -2$$

When the base is 10, the logarithm is a **Common Logarithm**.

If the base is not written, then it is automatically 10

$$\log 100 = 2$$

When the base is e , the logarithm is a **Natural Logarithm**

$$\log_e x = \ln x$$

$$y = \ln x \text{ iff } e^y = x$$

$$\ln 1 = 0$$

$$\ln e = 1$$

$$\ln e^x = x$$

$$\ln x = \ln y \rightarrow x = y$$

$$\log_a 1 = 0$$

$$\log_a a = 1$$

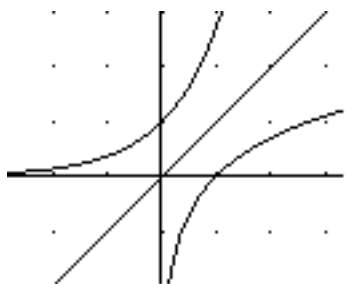
$$\log_a a^x = x$$

$$a^{\log_a x} = x$$

$$\log_a x = \log_a y \rightarrow x = y$$

$f(x) = a^x$ and $g(x) = \log_a x$ are inverses of each other

Their Graphs are reflections of each other through the line $y = x$



Assignment 127:

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