

Differentials:

dx represents the “Differential of x ”

To find the Differential of a Function, Find the Derivative, then multiply by the differential of the variable.

Let $y = \sin x$, then $dy = \cos x \, dx$

Let $y = \cos 2x$, then $dy = -\sin 2x \, 2dx$

Let $y = 3x^2 + 2x$, then $dy = (6x + 2) \, dx$

Antiderivatives:

The symbol for Antidifferentiation of $f(x)$ with respect to x is $\int f(x) \, dx$

$$\frac{d}{dx} ax = a$$

$$\int a \, dx = ax + C$$

$$\frac{d}{dx} u^n = nu^{n-1} \frac{du}{dx}$$

$$\int u^n \, du = \frac{1}{n+1} u^{n+1} + C$$

$$\frac{d}{dx} \sin u = \cos u \frac{du}{dx}$$

$$\int \cos u \, du = \sin u + C$$

$$\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}$$

$$\int \sin u \, du = -\cos u + C$$

$$\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}$$

$$\int \sec^2 u \, du = \tan u + C$$

$$\frac{d}{dx} \cot u = -\csc^2 u \frac{du}{dx}$$

$$\int \csc^2 u \, du = -\cot u + C$$

$$\frac{d}{dx} \sec u = \tan u \sec u \frac{du}{dx}$$

$$\int \tan u \sec u \, du = \sec u + C$$

$$\frac{d}{dx} \csc u = -\cot u \csc u \frac{du}{dx}$$

$$\int \cot u \csc u \, du = -\csc u + C$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\int e^u \, du = e^u + C$$

$$\frac{d}{dx} \ln(u) = \frac{1}{u} \frac{du}{dx}$$

$$\int \frac{du}{u} = \ln|u| + C$$

Find the Antiderivatives

1. $\int \cos u \, du =$

2. $\int \sin 2x \, dx =$

3. $\int 4x \cos(3x^2 + 2) \, dx =$

4. $\int \sin^5(3x - 1) \cos(3x - 1) \, dx =$

5. $\int \tan^4(2x + 7) \sec^2(2x + 7) \, dx =$

6. $\int \frac{3}{x} \, dx =$

7. $\int \cot(8x - 5) \, dx =$ Hint: $\cot x = \frac{\cos x}{\sin x}$

8. $\int 3x\sqrt{x^2 - 7} \, dx =$

9. $\int (3x^2 + 4x - 2)^{15} (3x + 2) \, dx =$

10. $\int \sin(\cos 2x) \sin 2x \, dx =$

11. $\int 2x \sec(3x^2 - 4) \tan(3x^2 - 4) \, dx =$