

111 Characteristics of Quadratic Functions

General Form of the Quadratic Function:

$$f(x) = ax^2 + bx + c, \text{ Where } a \text{ cannot be zero}$$

The value of a gives some of the information about the graph:

1. The Value of a gives vertical Stretch or Shrink.
2. If a is Negative then there is a Reflection about the x -axis.
3. For parent Quadratic Function, $a = 1, b = 0, c = 0$

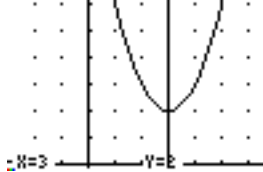
Vertex Form of the Quadratic Function:

$$f(x) = a(x - h)^2 + k, \text{ where } a \text{ cannot be zero. The position of the vertex is } (h, k), \text{ and the Axis of Symmetry is at } x = h.$$

Examples:

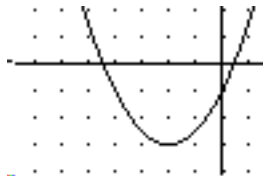
1. $f(x) = (x - 3)^2 + 2$

The Vertex is at $(3, 2)$. The Axis of Symmetry is $x = 3$ (A vertical Line)



2. $y = \frac{1}{2}(x + 2)^2 - 3$

The Vertex is at $(-2, -3)$. The Axis of Symmetry is $x = -2$ (A Vertical Line). Also, there is a Vertical Shrink of $\frac{1}{2}$.



3. Convert $f(x) = ax^2 + bx + c$ From General Form into Vertex Form by Completing the Square.

$f(x) = a\left(x^2 + \frac{b}{a}x + \right) + c$ The missing value is found by taking half the coefficient of the 2nd Term, then squaring the result. However, since this is inside the parentheses, it is automatically multiplied by a .

$$f(x) = a\left(x^2 + \frac{b}{a}x + \frac{b^2}{4a^2}\right) + c - \frac{b^2}{4a}$$

But This has a Perfect Square Trinomial and Can be Factored. We

will also find the common denominator of the outside terms, then Subtract Them.

$$f(x) = \left(x + \frac{b}{2a}\right)^2 - \frac{b^2 - 4ac}{4a}$$

The Vertex is at $\left(-\frac{b}{2a}, -\frac{b^2 - 4ac}{4a}\right)$ The axis of Symmetry is $x = -\frac{b}{2a}$.