

A104PC

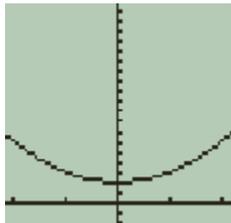
If  $f(x) = f(-x)$  for all values of  $x$ , then the function is an Even Function

Example:  $f(x) = x^2 + 2$  is an Even Function because

$$f(2) = 6 \text{ and } f(-2) = 6, f(5) = 27 \text{ and } f(-5) = 27$$

When you use opposite domain values, you get the same outcome.

If you graph an Even Function, you will see that it is symmetric about the y-axis



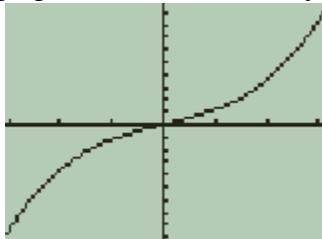
If  $f(x) = -f(-x)$  for all values of  $x$ , then the function is an Odd Function

Example:  $f(x) = x^3 + x$  is an Odd Function because

$$f(2) = 10 \text{ and } f(-2) = -10, f(1) = 2 \text{ and } f(-1) = -3$$

When you use opposite domain values, you get opposite outcomes.

If you graph an Odd Function, you will see that it is symmetric about the origin.



## Assignment 104

### 01.03 Graphs of Functions

Page 38, #'s 60, 61, 62, 64, 70, 93, 94, 103, 112, 120

Exer. 59-66: Algebraically determine whether the function is even, odd, or neither. Verify your answer using a graphing utility.

60.  $f(x) = x^6 - 2x^2 + 3$

61.  $g(x) = x^3 - 5x$

62.  $f(x) = x^3 - 5$

64.  $f(x) = x\sqrt{x+3}$

Exer. 67-72: Find the coordinates of a second point on the graph of a function  $f$  if the given point is on the graph and the function is (a) even and (b) odd.

70.  $(5, -1)$             (a)            (b)

Exer. 93-94: Determine whether the statement is true or false. Justify your answer.

93. A function with a square root cannot have a domain that is the set of all real numbers.

94. It is possible for an odd function to have the interval  $(0, \infty)$  as its domain.

103. If  $f$  is an even function, determine if  $g$  is even, odd, or neither. Explain.

a.  $g(x) = -f(x)$

b.  $g(x) = f(-x)$

c.  $g(x) = f(x) - 2$

d.  $g(x) = -f(x - 2)$

Exer. 111-114: Find

(a) the distance between the two points and

(b) the midpoint of the line segment joining the points.

112.  $(-5, 0), (3, 6)$

(a)

(b)

Exer. 119-120: Find the difference quotient and simplify your answer.

120.  $f(x) = 5 + 6x - x^2, \frac{f(6+h) - f(6)}{h} \quad h \neq 0$