

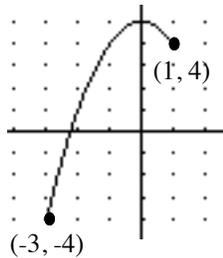
1. Interval Notation

$(3, 7]$ → All Real Numbers from 3 through 7, Not including 3, but including 7
This is a half open interval - Open on the left

$[-2, 9]$ → All Real Numbers from -2 through 9, including -2, and including 9
This is a closed interval

$(-10, 0)$ → All Real Numbers from -10 through 0, Not including -10 nor 0
This is an open interval

2. Find the Domain and Range



Domain: $[-3, 1]$

Range: $[-4, 5]$

3. Function Increasing on an Interval

If for any x_1 and x_2 on the interval, $x_1 < x_2 \rightarrow f(x_1) < f(x_2)$

4. Function Decreasing on an Interval

If for any x_1 and x_2 on the interval, $x_1 < x_2 \rightarrow f(x_1) > f(x_2)$

5. Constant Function on an Interval

If for any x_1 and x_2 on the interval, $f(x_1) = f(x_2)$

6. $f(a)$ is a Relative Maximum on an Interval (x_1, x_2)

If $\forall x \in (x_1, x_2), f(a) \geq f(x)$

7. $f(a)$ is a Relative Minimum on an Interval (x_1, x_2)

If $\forall x \in (x_1, x_2), f(a) \leq f(x)$

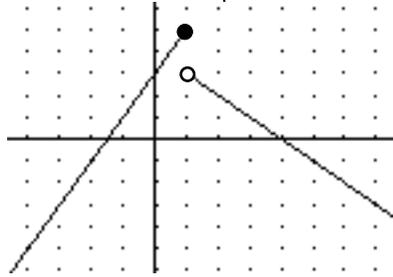
8. $f(x) = \lfloor x \rfloor$ – Greatest Integer Function (Floor Function)

$\lfloor x \rfloor$ is the Greatest Integer that is not Greater Than x

$\lfloor 3.2 \rfloor = 3$ $\lfloor 4 \rfloor = 4$ $\lfloor 5.9 \rfloor = 5$ $\lfloor -4.7 \rfloor = -5$

9. Piecewise Function

Example: $f(x) = \begin{cases} 2x + 3, & x \leq 1 \\ -x + 4, & x > 1 \end{cases}$



10. $f(x)$ is an Even Function

If $f(x) = f(-x) \forall x \in \text{the domain}$

Even Functions are symmetric about the y-axis

11. $f(x)$ is an Odd Function

If $f(-x) = -f(x) \forall x \in \text{the domain}$

Odd Functions are symmetric about the Origin

12. Assignment 003:

01.03 Graphs of Functions - Page 38, #'s 4, 8, 14a-h, 22, 34, 44, 48, 54

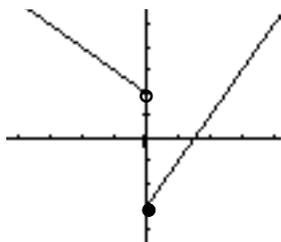
Pre-Calculus 1 Assignment 103

01.03 Graphs of Functions

Page 38, #'s 4, 8, 14a-h, 22, 34, 44, 48, 54

Exer. 1-4: Use the graph of the function to find the domain and range of f . Then find $f(0)$.

4.



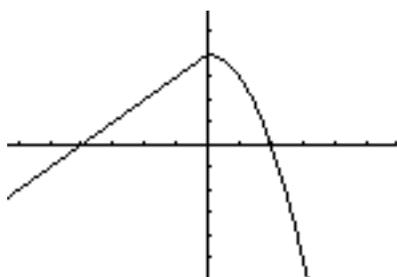
Exer. 5-10: Use a graphing utility to graph the function and estimate its domain and range. Then find the domain and range algebraically.

8. $h(t) = \sqrt{4 - t^2}$

Exer. 11-14: Use the given function to answer the questions.

- (a) Determine the domain of the function.
- (b) Find the value(s) of x such that $f(x) = 0$
- (c) The values of x from part (b) are referred to as what graphically?
- (d) Find $f(0)$, if possible.
- (e) The value from part (d) is referred to as what graphically?
- (f) What is the value of f at $x = 1$? What are the coordinates of the point?
- (g) What is the value of f at $x = -1$? What are the coordinates of the point?
- (h) The coordinates of the point on the graph of f at which $x = -3$, can be labeled $(-3, f(-3))$ or $(-3, \underline{\quad})$

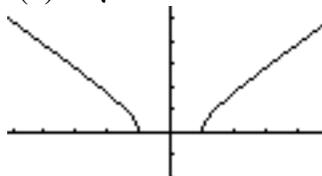
14.



$$f(x) = \begin{cases} x + 4, & \text{if } x \leq 0 \\ 4 - x^2, & \text{if } x > 0 \end{cases}$$

Exer. 19-22: Determine the open intervals over which the function is increasing, decreasing, or constant..

22. $f(x) = \sqrt{x^2 - 1}$



Exer. 31-36: Use a graphing utility to approximate any relative minimum or relative maximum values of the function.

$$34. \quad y = x^3 - 6x^2 + 15$$

Exer. 43-50: Sketch the graph of the piecewise defined function by hand.

$$44. \quad f(x) = \begin{cases} x + 6, & x \leq -4 \\ 2x - 4, & \text{if } x > -4 \end{cases}$$

$$48. \quad f(x) = \begin{cases} x + 5, & x \leq -3 \\ -2, & -3 < x < 1 \\ 5x - 4, & x \geq 1 \end{cases}$$

Exer. 51-56: Sketch the graph of the function by hand. Then use a graphing utility to verify the graph.

$$54. \quad f(x) = [|x - 2|] + 1$$